

Professional Course Examination, November/December 2019

(3rd Semester)

BACHELOR OF COMPUTER APPLICATIONS

Course : BCA-302

[Mathematics—III (Numerical Analysis)]

Full Marks : 75

Time : 3 hours

(PART : A—OBJECTIVE)

(Marks : 25)

The figures in the margin indicate full marks for the questions

SECTION—A

(Marks : 15)

Tick (✓) the correct answer in the brackets provided :

1×10=10

1. The relation between the operations E and ∇ is

(a) $\nabla = E - 1$ ()

(b) $E = \nabla^{\frac{1}{2}} - \nabla^{\frac{-1}{2}}$ ()

(c) $\nabla = 1 - E^{-1}$ ()

(d) $E = \nabla - 1$ ()

2. A numerical integration when applied to a function of a single variable is known as

- (a) quadratuple ()
- (b) quadrature ()
- (c) quarterback ()
- (d) None of the above ()

3. The order of convergence of regula-falsi method is

- (a) 1.218 ()
- (b) 1.518 ()
- (c) 1.618 ()
- (d) 1.718 ()

4. Given polynomial $x^3 - 2x^2 + x - 1$, then $\Delta^4 f(x)$ is equal to

- (a) 0 ()
- (b) 12 ()
- (c) $12x$ ()
- (d) 6 ()

5. The order of the differential equation $\left(\frac{dy}{dx}\right)^4 + 3y\frac{d^2y}{dx^2} = 0$ is

(a) 4 ()

(b) 2 ()

(c) 1 ()

(d) 3 ()

6. By using trapezoidal rule

$$\int_0^6 \frac{dx}{1+x}$$

is equal to

(a) 2.0432 ()

(b) 2.0314 ()

(c) 2.0414 ()

(d) 2.0214 ()

7. The number of subintervals required in Simpson's $\frac{3}{8}$ -th rule is a multiple of

(a) 6 ()

(b) 2 ()

(c) 3 ()

(d) 1 ()

8. In bisection method, the convergence is

- (a) linear ()
- (b) very fast ()
- (c) quadratic ()
- (d) very slow ()

9. $\mu + \frac{1}{2} \delta$ is equal to

- (a) $\mu\delta$ ()
- (b) $E^{\frac{1}{2}}$ ()
- (c) $\nabla\Delta$ ()
- (d) $E^{-\frac{1}{2}}$ ()

10. The process of computing the value of the function outside the given range is called

- (a) extrapolation ()
- (b) interpolation ()
- (c) intervention ()
- (d) None of the above ()

Indicate whether the following statements are *True (T)* or *False (F)* by putting a Tick (✓) mark in the brackets provided :

1×5=5

1. The degree of $\left(\frac{d^2y}{dx^2}\right)^3 + 2\left(\frac{dy}{dx}\right)^4 + 9 = \sin x$ is 3.

(T / F)

2. If $f(x)$ is a transcendental function like $a + be^x + c \sin x + d \log x$, etc., the solution is exact.

(T / F)

3. $E\nabla = \nabla = \nabla E$.

(T / F)

4. The formula for Taylor's method is

$$y = y_0 + (x - x_0)(y')_0 + \frac{(x - x_0)^2}{2!}(y'')_0 + \frac{(x - x_0)^3}{3!}(y''')_0 + \dots \dots$$

(T / F)

5. Gauss forward interpolation formula employs odd differences below the central line.

(T / F)

SECTION—B

(Marks : 10)

Answer the following questions :

2×5=10

1. Write the formula for Newton's forward interpolation formula.
2. Prove that $\Delta^3 y_2 = \nabla^3 y_5$.
3. Express $y = 2x^3 - 3x^2 + 3x - 10$ in factorial notation.
4. Verify that $y = A \cos x - B \sin x$ is a solution of the differential equation

$$\frac{d^2 y}{dx^2} + y = 0$$

5. Write the formula for Lagrange's inverse interpolation formula.